

Introduction to modeling, simulation and data science in oncology

3. Introduction to Statistical Learning

S. Benzekry

Formation « Ecole doctorale Mathématiques et Informatique »



Modeling in ONCology

Ok Google: What is AI??

Definition: A **computer** system able to perform tasks that normally require human **intelligence**, such as visual perception, speech recognition, decision-making, and translation between languages.

Oxford dictionary

- Exists since decades

- New « hype » since ~2011 mostly thanks to :

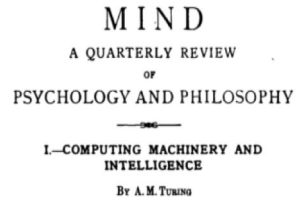
- **Computing power**

- **Big data**

Deep Learning



Enigma



Turing, Mind, 1950



Google DeepMind, Nature, 2016

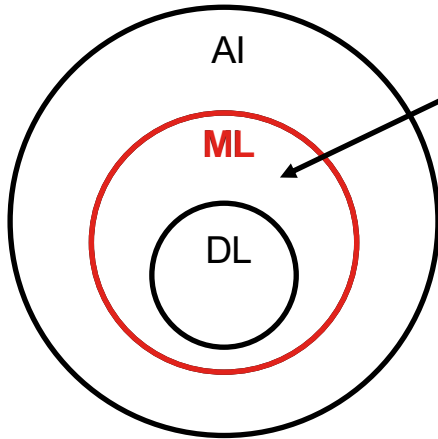


©Information Age, ACS

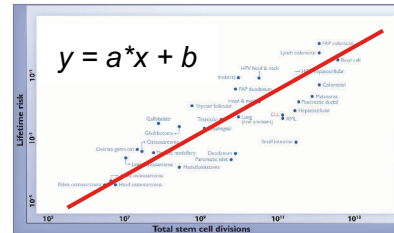
Artificial Intelligence, Machine Learning and Deep Learning

ML = machine (automatic) learning

Goal = predict outcome y as a function of input/features x_1, \dots, x_n



x_1, x_2, x_3 —

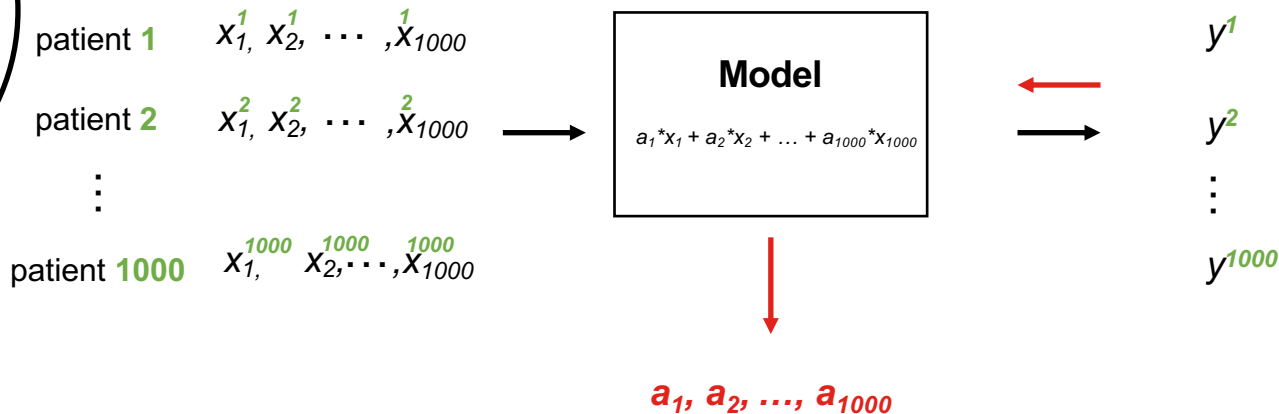
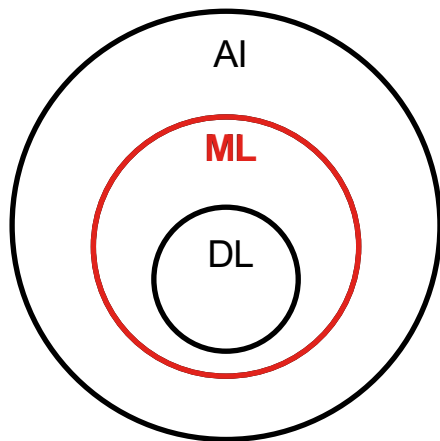


→ y

Artificial Intelligence, Machine Learning and Deep Learning

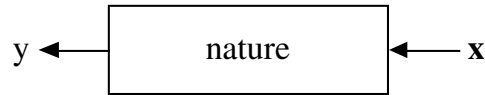
Supervised machine learning

Predict outcome y as a function of *a lot* of input/features x_1, \dots, x_n (big data, high dimensional statistics)

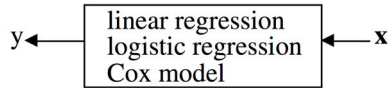


Statistical Modeling: The Two Cultures

Leo Breiman



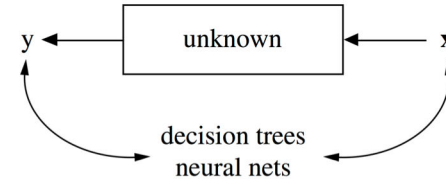
The data modeling culture



Model validation. Yes–no using **goodness-of-fit tests and residual examination.**

Estimated culture population. 98% of all statisticians.

The algorithmic modeling culture



Model validation. Measured by **predictive accuracy.**
Estimated culture population. 2% of statisticians, many in other fields.

Statistical (Machine) Learning

$$Y = M(x) + \varepsilon$$

- Goal = predict Y = find M
- Y quantitative \Rightarrow regression
- Y qualitative \Rightarrow classification
- Learning = use data
 - only x values \Rightarrow unsupervised learning
 - (x, y) examples \Rightarrow supervised learning

3.1 Classification

Confusion matrix

$$\text{Data} \begin{pmatrix} x^1 \\ \vdots \\ x^N \end{pmatrix} \longrightarrow \text{Predictions} \begin{pmatrix} \hat{y}^1 \\ \vdots \\ \hat{y}^N \end{pmatrix} = \begin{pmatrix} \hat{M}(x^1) \\ \vdots \\ \hat{M}(x^N) \end{pmatrix} \text{ vs reality} \begin{pmatrix} y^1 \\ \vdots \\ y^N \end{pmatrix}$$

Actual

	1	0
+	TP (Sensitivity)	FP
-	FN	TN (Specificity)

Model

$$\text{Accuracy} = \frac{TP+TN}{TP+TN+FP+FN}$$

$$\text{Sensitivity} = SE = \mathbb{P}(+|1) = TPR = \frac{TP}{TP+FN}$$

$$\beta = \mathbb{P}(-|1) = FNR = 1 - SE = \text{proba of type II error}$$

(classify as benign what is cancer)

$$\text{Specificity} = SP = \mathbb{P}(-|0) = TNR = \frac{TN}{FP+TN}$$

$$\alpha = \mathbb{P}(+|0) = FPR = 1 - SP = \text{proba of type I error}$$

(classify as tumor what is benign)

Positive and negative predictive value

- Sensitivity and specificity are **not sufficient** to assess a model
- We are often more interested in $\mathbb{P}(1|+)$ (= **positive predictive value**, *PPV*) and $\mathbb{P}(0|-)$ (= **negative predictive value**, *NPV*)
- From Bayes

p prevalence
↓

$$PPV = \mathbb{P}(1|+) = \frac{\mathbb{P}(+|1)\mathbb{P}(1)}{\mathbb{P}(+)}$$

$$\begin{aligned}\mathbb{P}(+) &= \mathbb{P}(+|0)\mathbb{P}(0) + \mathbb{P}(+|1)\mathbb{P}(1) = (1 - \mathbb{P}(-|0))(1 - \mathbb{P}(1)) + SE \cdot \mathbb{P}(1) \\ &= (1 - SP) \cdot (1 - p) + SE \cdot p\end{aligned}$$

$$PPV = \frac{SE \cdot p}{(1 - SP) \cdot (1 - p) + SE \cdot p}$$

- Other metrics: $F1$ = harmonic mean of *PPV* (precision) and sensitivity (recall) = $2(PPV^{-1} + SE^{-1})^{-1}$

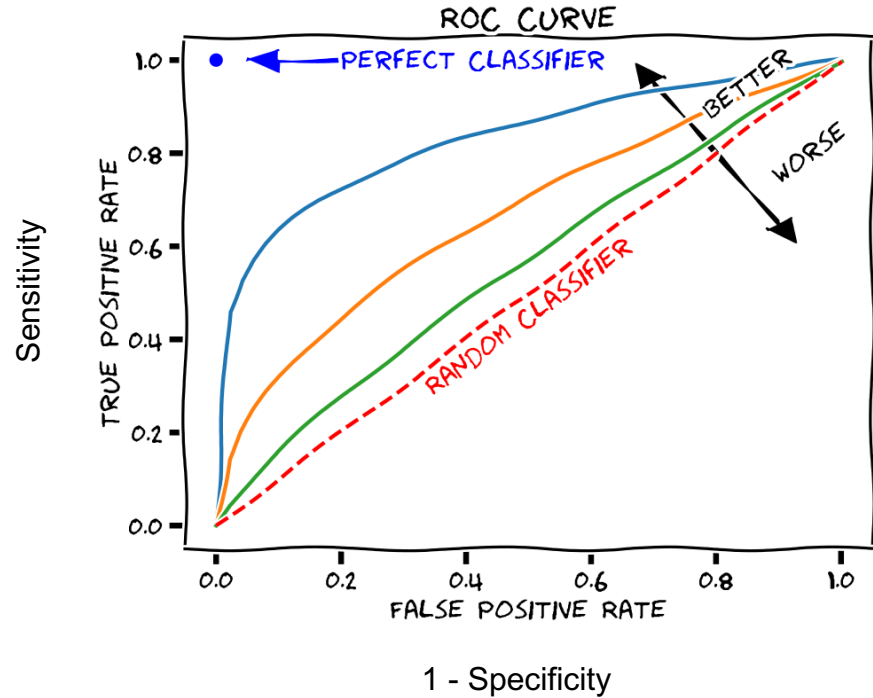
Example: Lung cancer and smoking status

- Percentage of smokers among lung cancer patients = 90%, i.e. SE of a model based on smoking status is 0.9
- Approx. 30% of population is composed of smokers $\Rightarrow SP (= TNR, \text{i.e. proportion of people who don't smoke and don't have cancer})$ is 70%.
- Assuming a lifetime risk of having lung cancer of 7.19% (= prevalence)

$$PPV = \mathbb{P}(\text{lung cancer during lifetime} \mid \text{smoker}) = 18.9\%$$

ROC curve analysis

- In practical cases a classification model often assigns a **score** (e.g. proba)
- For each value of a **threshold**, one *SE* and one *SP* value
- Global quantification of performances = **area under the curve** (AUC)



Interpretation of AUC

AUC = probability that a random pair of predictions (\hat{y}^1, \hat{y}^2) is **concordant** with the observations i.e that the score of \hat{y}^1 is larger than the score of \hat{y}^2 if $y^1 > y^2$.

- S_1 = score in class we want to classify as positive (say, malignant), density f_1
- S_0 = score in other class (say, healthy/benign), density f_0
- T = threshold

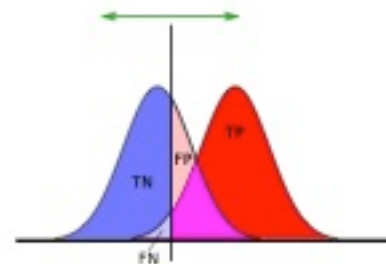
$$AUC = \int_{T_{max}}^{T_{min}} SE(T) d(FPR(T))$$

$$SE(T) = \mathbb{P}(S \geq T|1) = \int_T^{T_{max}} f_1(x) dx$$

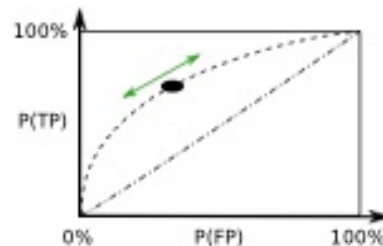
$$FPR(T) = \mathbb{P}(S \geq T|0) = \int_T^{T_{max}} f_0(x) dx$$

$$AUC = \int_{T_{min}}^{T_{max}} \int_T^{T_{max}} f_1(x) f_0(T) dT$$

$$= \mathbb{P}(S_1 \geq S_0)$$



TP	FP
FN	TN



Logistic regression

$$p = \mathbb{P}(Y = 1) \in (0,1) \xrightarrow{?} \mathbb{R}$$

$$\frac{p}{1-p} \in (0, +\infty) = \frac{\mathbb{P}(Y = 1)}{\mathbb{P}(Y = 0)} = \text{odds} \approx \text{chance}$$

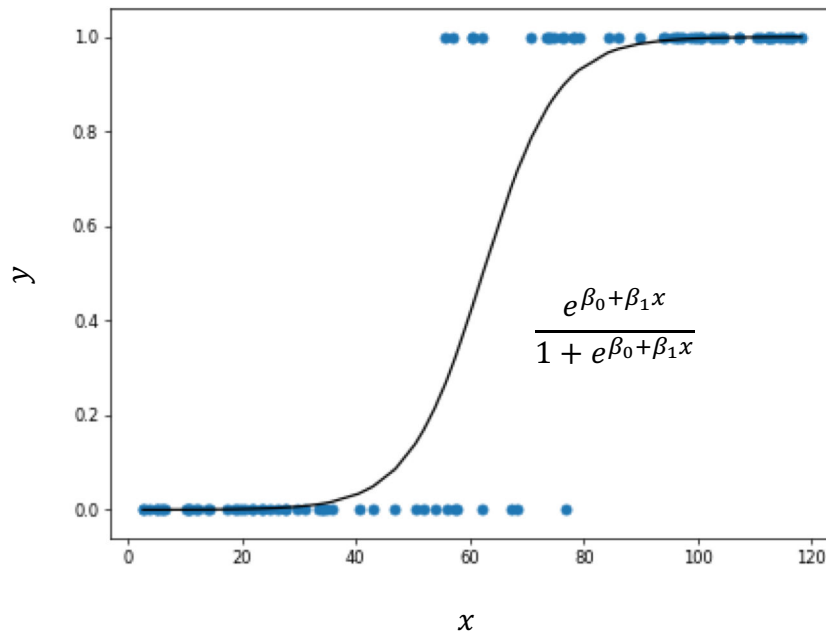
$$\ln\left(\frac{p}{1-p}\right) = \beta_0 + \beta_1 x_1 + \dots + \beta_L x_L$$

$$\Leftrightarrow p = \frac{e^{\beta_0 + \beta_1 x_1 + \dots + \beta_L x_L}}{1 + e^{\beta_0 + \beta_1 x_1 + \dots + \beta_L x_L}} = \pi(x)$$

Estimation: **likelihood maximization**

Interpretation: for one variable x , $\text{odds}(x) = e^{\beta_0 + \beta_1 x}$

$$\Rightarrow \beta = \frac{\text{odds}(x+1)}{\text{odds}(x)} = \text{odds ratio} = OR$$

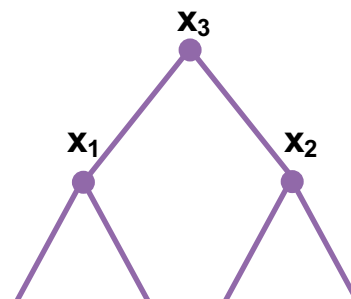
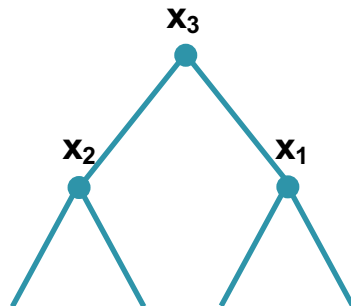
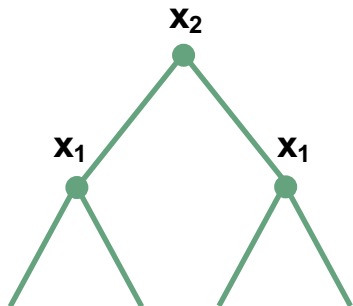
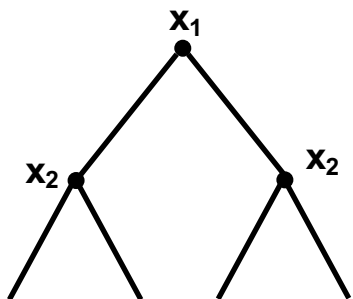
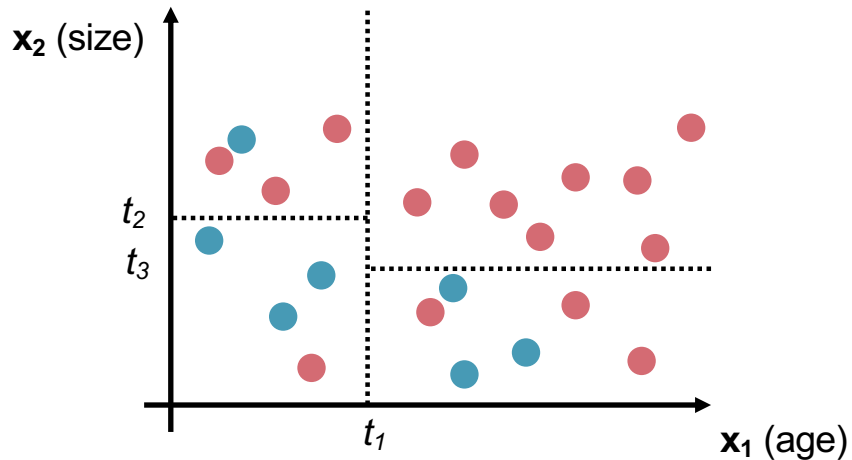
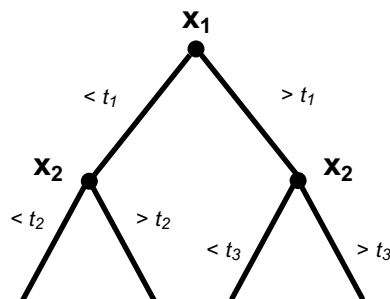


if $OR = 1.5$ there is a 50% increase of chance of having $Y = 1$ for an increase of x of one unit

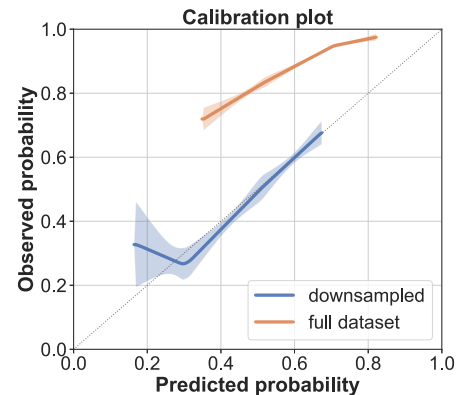
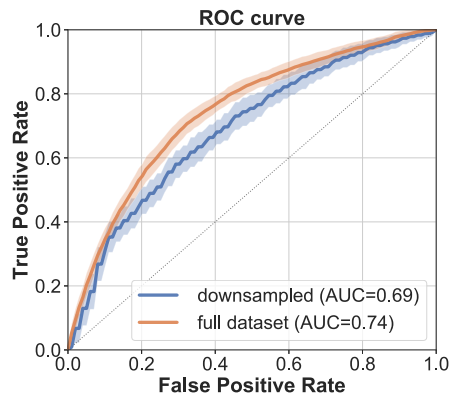
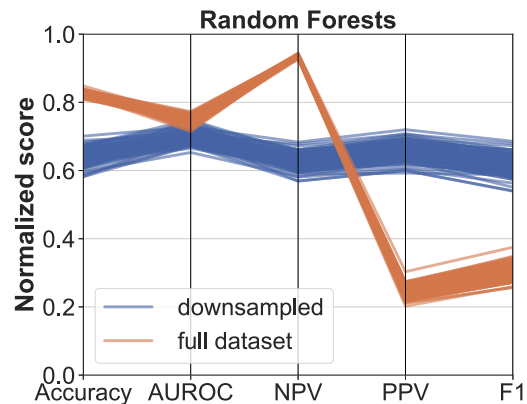
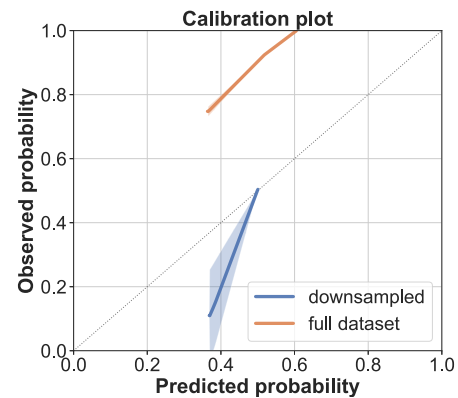
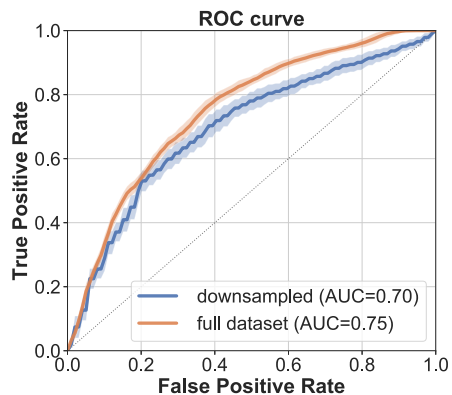
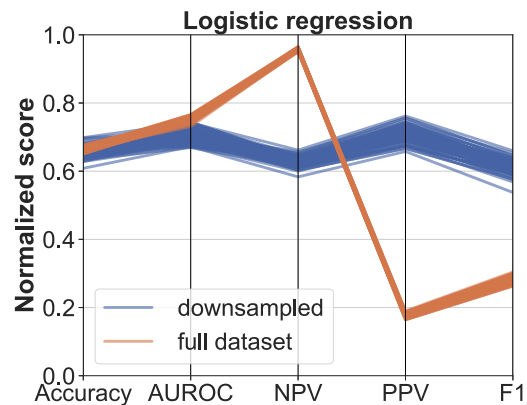
Random Forests

● = Tumor
● = Benign

- Binary **classification/regression tree**
- Sample dataset and choose splitting features randomly to get a **forest**
- Vote/average over trees

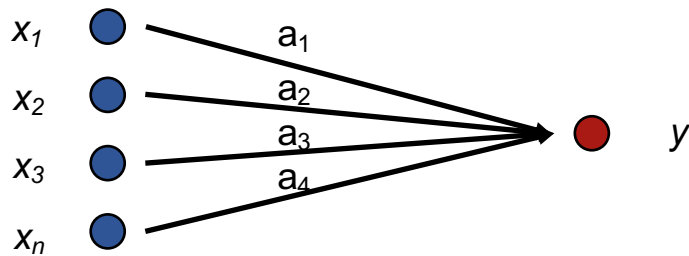
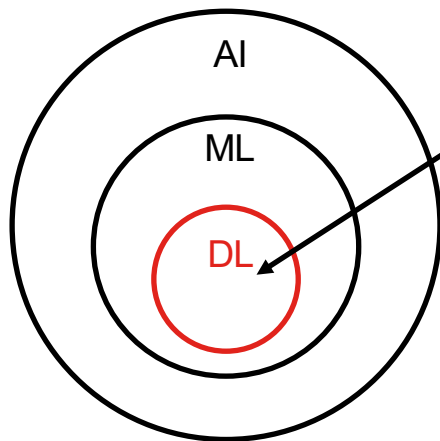


Prediction results



Neural networks

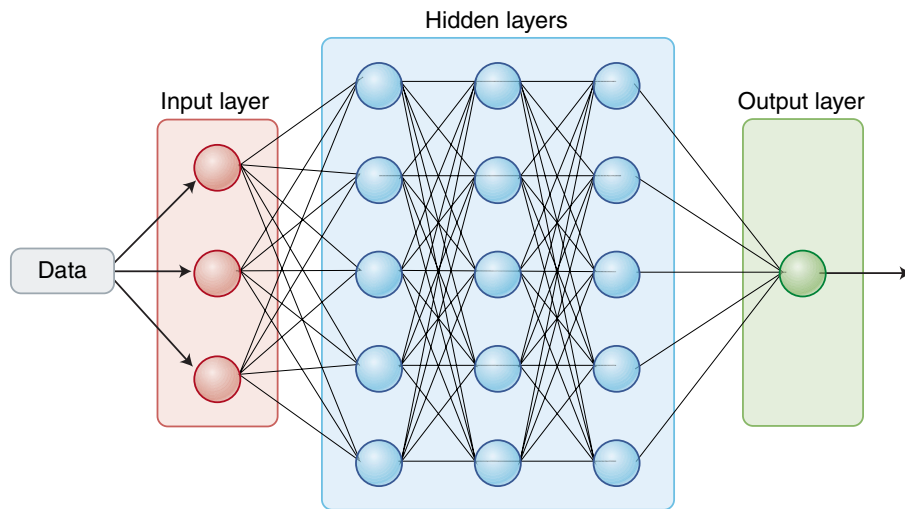
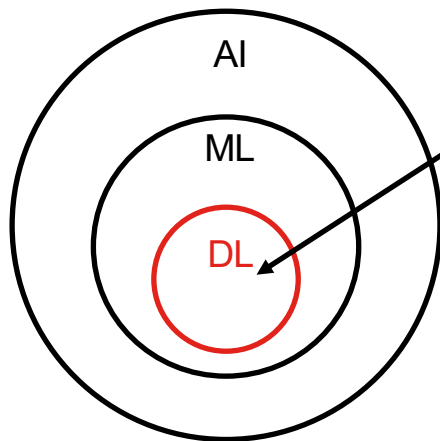
DL: artificial neural networks



$$y = f(b + a_1x_1 + \dots + a_nx_n), f = \text{logistic, softmax, } \dots$$

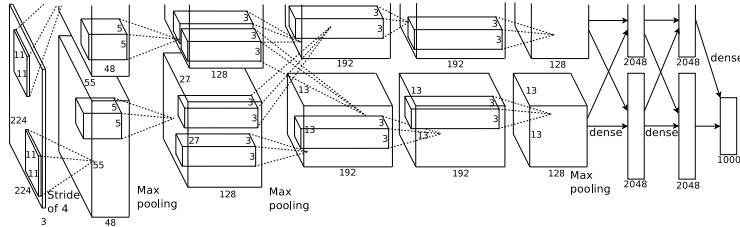
Neural networks

DL: artificial neural networks



Success example of DL: computer vision

- 1.2 million images (ImageNet, Stanford) used to train a deep convolutional neural network



©Science Etonnante

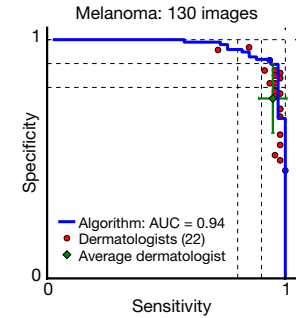
2010		2011	
1. NEC	28%	1. XRCE	26%
2. XRCE	34%	2. Uv A	31%
3. ISIL	45%	3. ISI	36%
4. UCI	47%	4. NII	50%
5. Hminmax	54%		

2012		2013	
1. SuperVision	16%	1. Clarifai	12%
2. ISI	26%	2. NUS	13%
3. VGG	27%	3. ZeilerFergus	13%
4. XRCE	27%	4. A.Howard	13%
5. Uv A	30%	5. OverFeat	14%

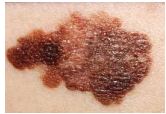
Krizhevsky, A. et al. ImageNet classification with deep convolutional neural networks, NIPS, 2012

Classification of skin lesions

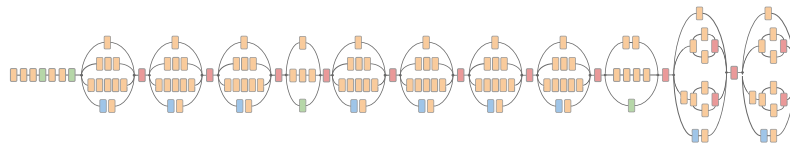
- 129 450 annotated images
- Task = prediction **benign/malignant**
- Similar performances as dermatologists



Skin lesion image



Deep convolutional neural network (Inception v3)



- Convolution
- AvgPool
- MaxPool
- Concat
- Dropout
- Fully connected
- Softmax

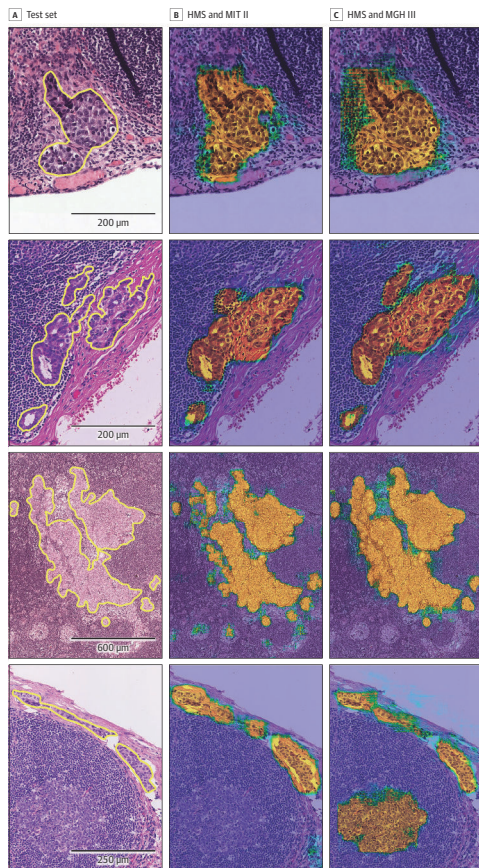
Training classes (757)

- Acral-lentiginous melanoma
- Amelanotic melanoma
- Lentigo melanoma
- ...
- Blue nevus
- Halo nevus
- Mongolian spot
- ...
- ...
- ...
- ...

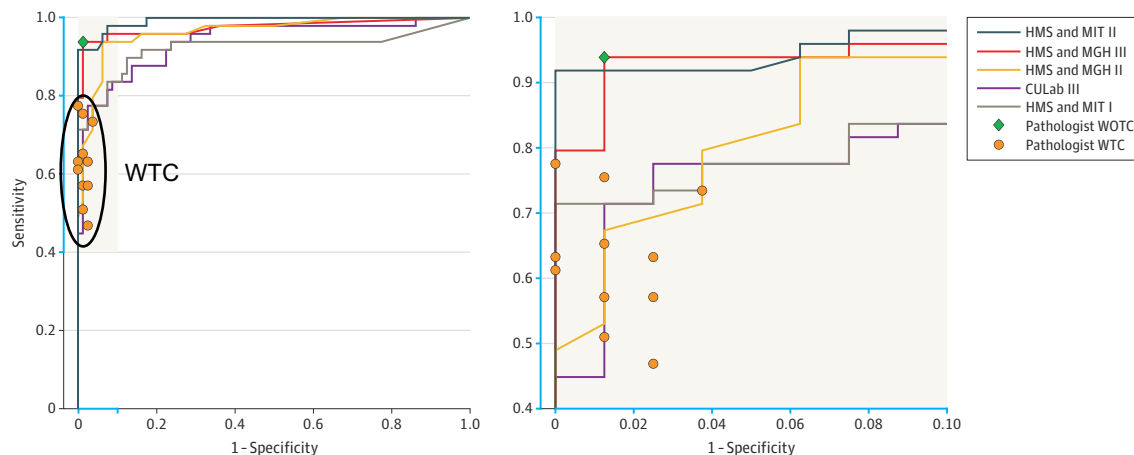
Inference classes (varies by task)

- 92% malignant melanocytic lesion
- 8% benign melanocytic lesion

Detection of lymph node metastases from histological images

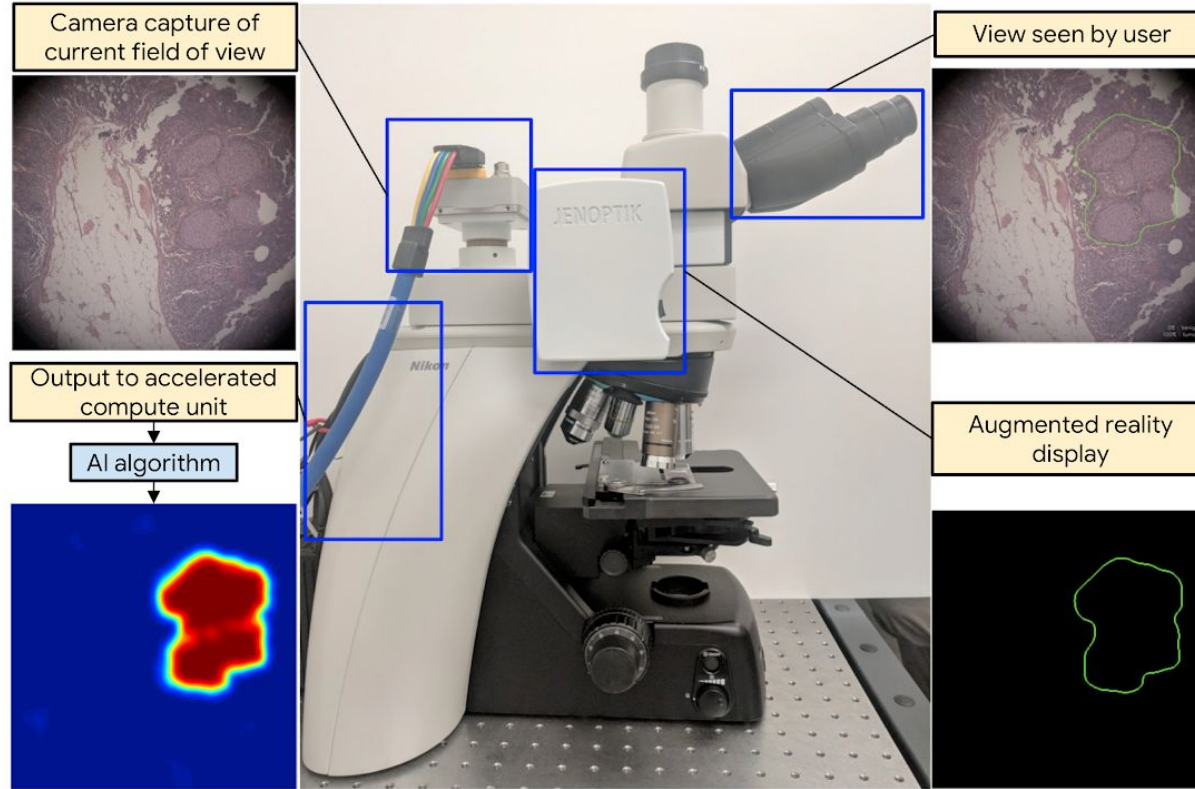


- One pathology slide = **several gigapixels**
- Best algorithms of the challenge = Deep Learning
- Same performances as pathologists **without time constraint**, but significantly better than 11 pathologists with constraint (WTC)

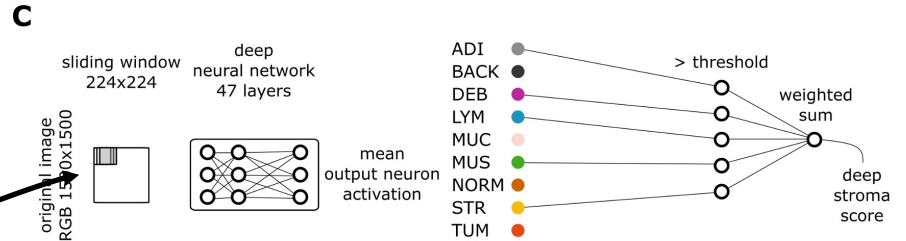
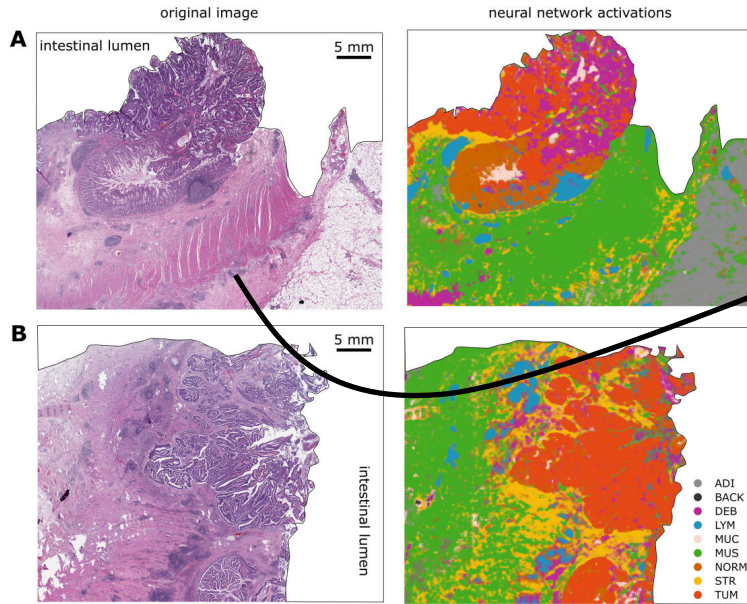


Bejnordi et al., Diagnostic Assessment of Deep Learning Algorithms for Detection of Lymph Node Metastases in Women With Breast Cancer, JAMA, 2017

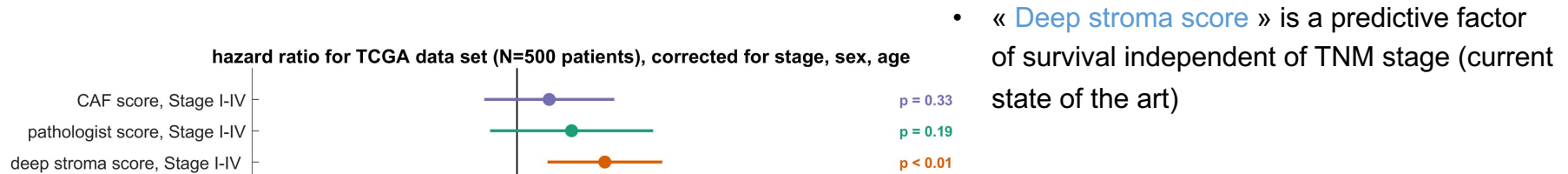
Microscope 2.0



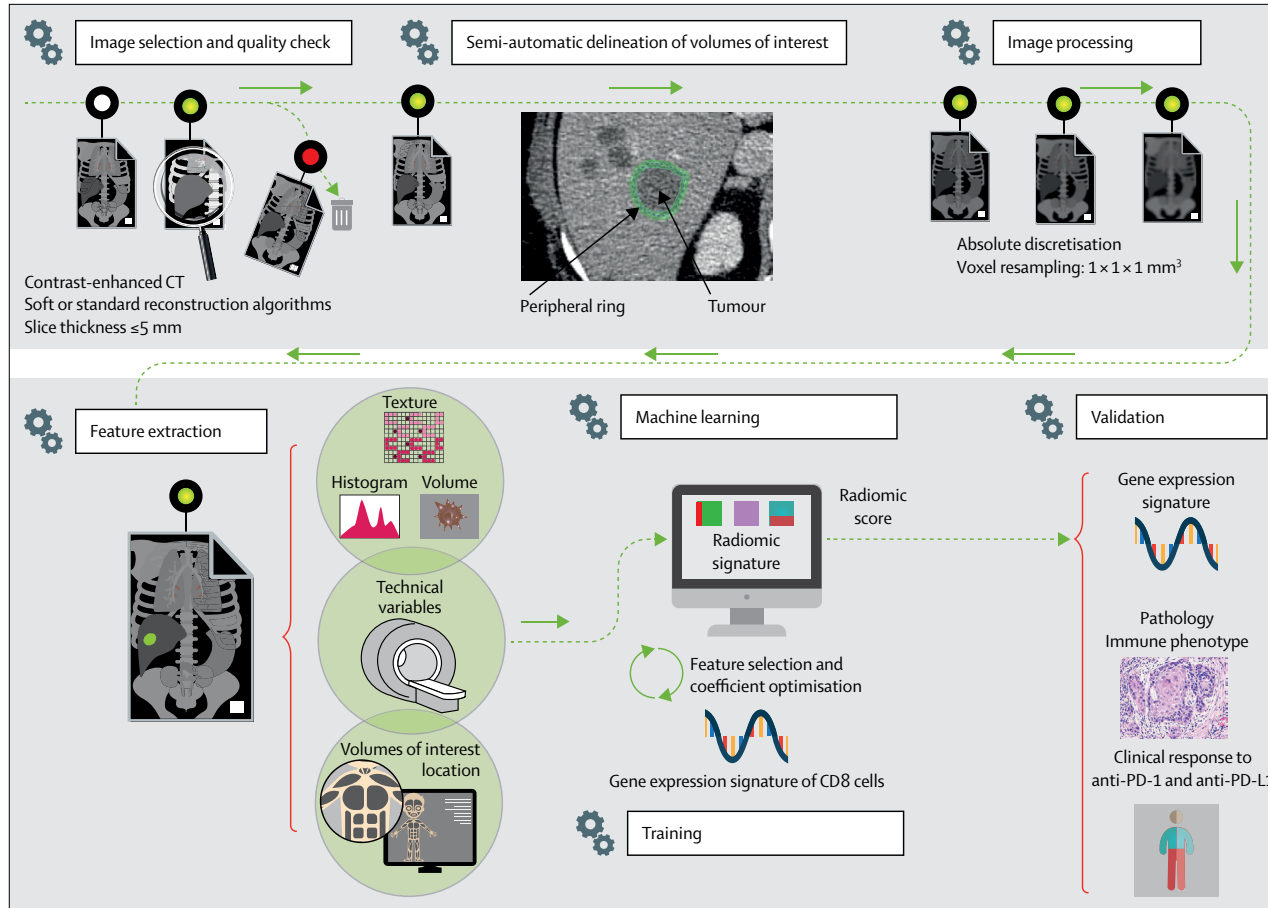
Quantitative analysis of histopathological slides in CRC



- 100,000 patches of histological slides
- Stroma
- 94% classification accuracy on test data set



Prediction of response to immune-checkpoint inhibition



Prediction of response to immune-checkpoint inhibition

but....

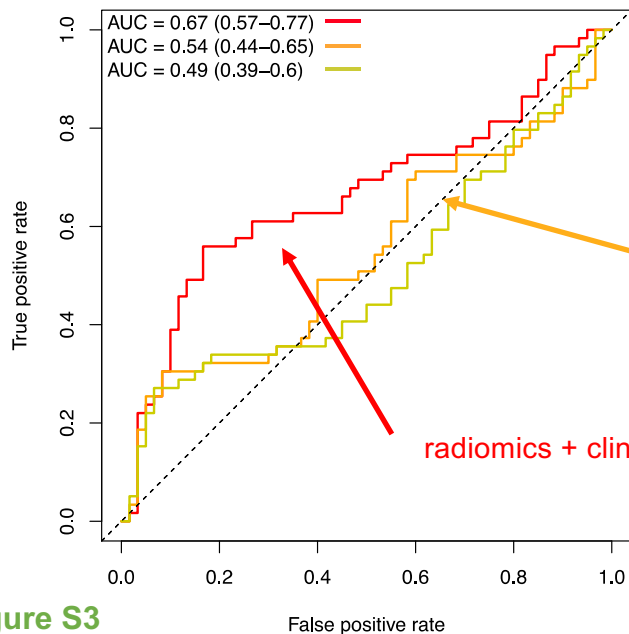


Figure S3



Original article
 Vulnerabilities of radiomic signature development: The need for safeguards

Mattea L. Welch^{a,f,i}, Chris McIntosh^{e,f,i}, Benjamin Haibe-Kains^{a,c,i,j}, Michael F. Milosevic^{b,e,i}, Leonard Wee^g, Andre Dekker^g, Shao Hui Huang^{b,i}, Thomas G. Purdie^{b,e,f,i}, Brian O'Sullivan^{b,i}, Hugo J.W.L. Aerts^h, David A. Jaffray^{a,b,d,e,f,i,*}

^aDepartment of Medical Biophysics, University of Toronto; ^bDepartment of Radiation Oncology, University of Toronto; ^cOntario Institute of Cancer Research, Toronto; ^dIBBME, University of Toronto; ^eRadiation Medicine Program, Princess Margaret Cancer Centre, Toronto; ^fThe Techna Institute for the Advancement of Technology for Health, Toronto, Canada; ^gDepartment of Radiation Oncology (MAASTRO), GROW Research Institute, Maastricht University, the Netherlands; ^hDana-Farber Cancer Institute, Brigham and Women's Hospital.

ABSTRACT

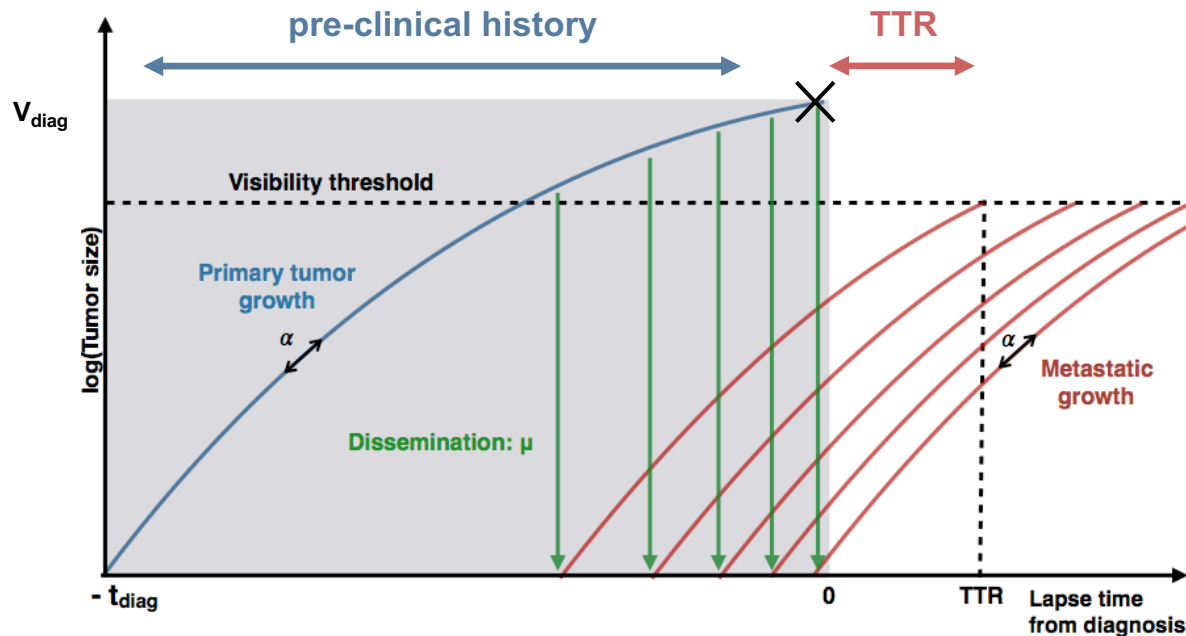
Purpose: Refinement of radiomic results and methodologies is required to ensure progression of the field. In this work, we establish a set of safeguards designed to improve and support current radiomic methodologies through detailed analysis of a radiomic signature.

Methods: A radiomic model (MW2018) was fitted and externally validated using features extracted from previously reported lung and head and neck (H&N) cancer datasets using gross-tumour-volume contours, as well as from images with randomly permuted voxel index values; i.e. images without meaningful texture. To determine MW2018's added benefit, the prognostic accuracy of tumour volume alone was calculated as a baseline.

Results: MW2018 had an external validation concordance index (c-index) of 0.64. However, a similar performance was achieved using features extracted from images with randomized signal intensities (c-index = 0.64 and 0.60 for H&N and lung, respectively). Tumour volume had a c-index = 0.64 and correlated strongly with three of the four model features. It was determined that the signature was a surrogate for tumour volume and that intensity and texture values were not pertinent for prognostication.

Conclusion: Our experiments reveal vulnerabilities in radiomic signature development for prognostication. suggest safeguards that can be used to refine methodologies, and ensure productive radiomic development using objective and independent features.

Mechanistic modeling of time to relapse



- Number of metastases with size larger than the **visible size V_{vis}**

$$N_{vis}(t) = \int_{V_{vis}}^{+\infty} \rho(t, v) dv$$

$$= \int_0^{t - \tau_{vis}} d(V_p(t)) dt$$

τ_{vis} = time to reach V_{vis}

- Time to relapse (TTR)** = time elapsed from diagnosis to the appearance of a first visible metastasis

$$TTR = \inf \{t > 0 : N_{vis}(t_{diag} + t) \geq 1\}$$

- Parameter β fixed such that $V_{\infty} = e^{\frac{\alpha}{\beta}} = 10^{12}$ cells

Mixed-effects statistical model

$$\ln(T^i) = \ln\left(TTR(V_{diag}^i; \alpha^i, \mu^i)\right) + \varepsilon^i, \quad \varepsilon^i \sim \mathcal{N}(0, \sigma^2) \quad (\text{Observation model})$$

$$S(t|\alpha^i, \mu^i) = \mathbb{P}(T^i > t|\alpha^i, \mu^i)$$

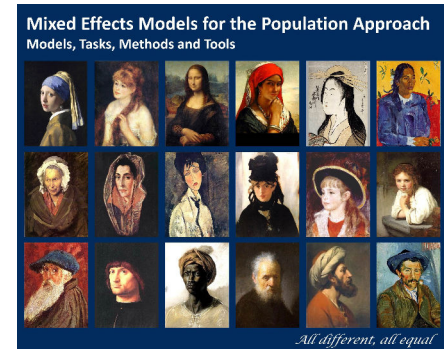
Survival function to account for **censoring** in the likelihood

$$\ln(\alpha^i) = \ln(\alpha_{pop}) + \eta_{\alpha}^i, \quad \eta_{\alpha}^i \sim \mathcal{N}(0, \omega_{\alpha}^2)$$

$$\ln(\mu^i) = \ln(\mu_{pop}) + \eta_{\mu}^i, \quad \eta_{\mu}^i \sim \mathcal{N}(0, \omega_{\mu}^2)$$

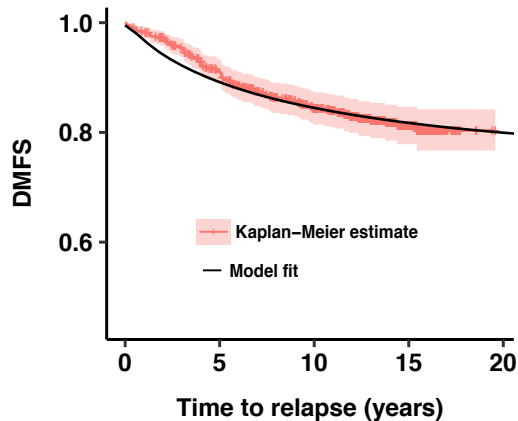
Likelihood maximization performed using the SAEM algorithm implemented in the *saemix* R package

Comets, Lavenu, Lavielle, J Stat Softw, 2017

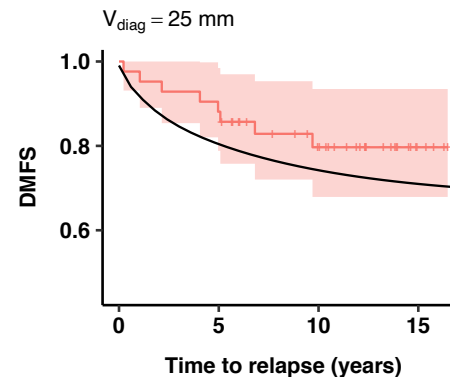
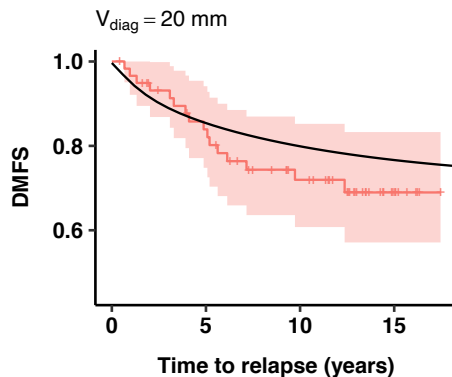
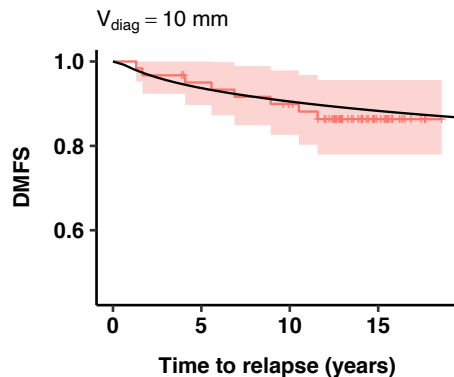


Lavielle, CRC press, 2014

Descriptive power: fit to the data



Parameter	Estimate	r.s.e. (%)
$\log \alpha_{pop}$	-6.34	12.6
$\log \mu_{pop}$	-26.8	3.68
σ	0.542	28.4
ω_{α}	3.37	36.4
ω_{μ}	3.78	15.9

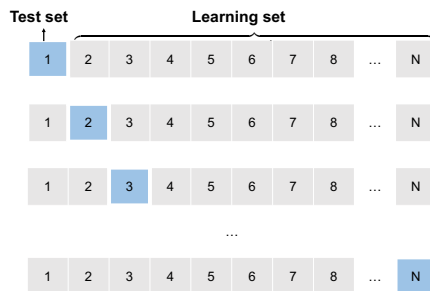
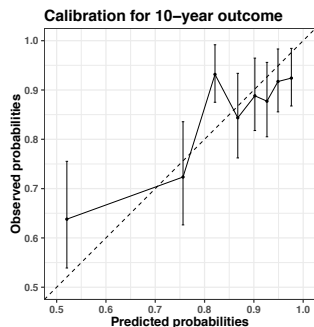


Predictive power: covariates

$$\ln(\mu^i) = \ln(\mu_{pop}) + \beta_{\mu}^T \mathbf{x}_{\mu}^i + \eta_{\mu}^i, \quad \eta_{\mu}^i \sim \mathcal{N}(0, \omega_{\mu}^2)$$

$$\ln(\alpha^i) = \ln(\alpha_{pop}) + \beta_{\alpha}^T \mathbf{x}_{\alpha}^i + \eta_{\alpha}^i, \quad \eta_{\alpha}^i \sim \mathcal{N}(0, \omega_{\alpha}^2)$$

Parameter	Estimate	r.s.e. (%)	p-value
$\log \alpha_{pop}$	-8.883	10.151	
$\beta_{\text{Ki67}, \alpha}$	0.086	27.376	$2.59 \cdot 10^{-4}$
$\beta_{\text{HER2}, \alpha}$	0.029	42.833	0.020
$\beta_{\text{CD44}, \alpha}$	0.011	60.816	0.1
$\beta_{\text{TRIO}, \alpha}$	0.016	58.119	0.085
$\log \mu_{pop}$	-26.342	3.696	
$\beta_{\text{EGFR}, \mu}$	0.039	47.527	0.035
σ	0.606	23.104	
ω_{α}	2.062	22.715	
ω_{μ}	3.563	16.759	



c-index = 0.67
(10-folds cross-validation)

Patient ID	Tumor size (mm)	Ki67	HER2	CD44	TRIO	EGFR	Observed TTR (cens)	Predicted TTR	Prediction error (days)
255	25	1	60	90	60	0	1812 (1)	1609	203
47	20	32	100	0	0	50	739 (1)	447	292
143	18	60	0	50	0	0	2798 (1)	434	2364
12	10	20	0	23	0	0	5970 (0)	$+\infty$	-

Comparison of predictive metrics

5 years metastatic-free survival

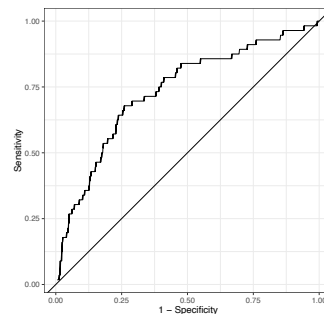
	AUROC	Accuracy	PPV	NPV
RSF	0.75	0.90	0.71	0.71
Mechanistic model	0.73	0.90	0.72	0.70
Cox	0.75	0.91	0.77	0.71

10 years metastatic-free survival

	AUROC	Accuracy	PPV	NPV
RSF	0.69	0.82	0.68	0.66
Mechanistic model	0.69	0.81	0.71	0.64
Cox	0.71	0.82	0.70	0.68

other tested ML models (support vector machine, k-nearest neighbors, gradient boosting) had similar or worse performances

Mechanistic



RSF

